

Study Guide and Intervention

7NS2.4

Square Roots

The square root of a number is one of two equal factors. The radical sign $\sqrt{\quad}$ is used to indicate the positive square root.

Examples**Find each square root.**

1 $\sqrt{1}$

Since $1 \cdot 1 = 1$, $\sqrt{1} = 1$.

2 $-\sqrt{16}$

Since $4 \cdot 4 = 16$, $-\sqrt{16} = -4$.

3 $\sqrt{0.25}$

Since $0.5 \cdot 0.5 = 0.25$, $\sqrt{0.25} = 0.5$.

4 $\sqrt{\frac{25}{36}}$

Since $\frac{5}{6} \cdot \frac{5}{6} = \frac{25}{36}$, $\sqrt{\frac{25}{36}} = \frac{5}{6}$.

Example 5**Solve $a^2 = \frac{4}{9}$.**

$a^2 = \frac{4}{9}$

Write the equation.

$\sqrt{a^2} = \sqrt{\frac{4}{9}}$

Take the square root of each side.

$a = \frac{2}{3}$ or $-\frac{2}{3}$

Notice that $\frac{2}{3} \cdot \frac{2}{3} = \frac{4}{9}$ and $(-\frac{2}{3})(-\frac{2}{3}) = \frac{4}{9}$.

The equation has two solutions, $\frac{2}{3}$ and $-\frac{2}{3}$.**Exercises****Find each square root.**

1. $\sqrt{4}$ **2**

2. $\sqrt{9}$ **3**

3. $-\sqrt{49}$ **-7**

4. $-\sqrt{25}$ **-5**

5. $\sqrt{0.01}$ **0.1**

6. $-\sqrt{0.64}$ **-0.8**

7. $\sqrt{\frac{9}{16}}$ **$\frac{3}{4}$**

8. $-\sqrt{\frac{1}{25}}$ **$-\frac{1}{5}$**

ALGEBRA Solve each equation.

9. $x^2 = 121$ **11 or -11**

10. $a^2 = 3,600$ **60 or -60**

11. $p^2 = \frac{81}{100}$ **$\frac{9}{10}$ or $-\frac{9}{10}$**

12. $t^2 = \frac{121}{196}$ **$\frac{11}{14}$ or $-\frac{11}{14}$**

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Estimating Square Roots

Most numbers are not perfect squares. You can estimate square roots for these numbers.

Example 1 Estimate $\sqrt{204}$ to the nearest whole number.

- The first perfect square less than 204 is 14.
- The first perfect square greater than 204 is 15.

$$196 < 204 < 225 \quad \text{Write an inequality.}$$

$$14^2 < 204 < 15^2 \quad 196 = 14^2 \text{ and } 225 = 15^2$$

$$14 < \sqrt{204} < 15 \quad \text{Take the square root of each number.}$$

So, $\sqrt{204}$ is between 14 and 15. Since 204 is closer to 196 than 225, the best whole number estimate for $\sqrt{204}$ is 14.

Example 2 Estimate $\sqrt{79.3}$ to the nearest whole number.

- The first perfect square less than 79.3 is 64.
- The first perfect square greater than 79.3 is 81.

$$64 < 79.3 < 81 \quad \text{Write an inequality.}$$

$$8^2 < 79.3 < 9^2 \quad 64 = 8^2 \text{ and } 81 = 9^2$$

$$8 < \sqrt{79.3} < 9 \quad \text{Take the square root of each number.}$$

So, $\sqrt{79.3}$ is between 8 and 9. Since 79.3 is closer to 81 than 64, the best whole number estimate for $\sqrt{79.3}$ is 9.

Exercises

Estimate to the nearest whole number.

1. $\sqrt{8}$ **3**

2. $\sqrt{37}$ **6**

3. $\sqrt{14}$ **4**

4. $\sqrt{26}$ **5**

5. $\sqrt{62}$ **8**

6. $\sqrt{48}$ **7**

7. $\sqrt{103}$ **10**

8. $\sqrt{141}$ **12**

9. $\sqrt{14.3}$ **4**

10. $\sqrt{51.2}$ **7**

11. $\sqrt{82.7}$ **9**

12. $\sqrt{175.2}$ **13**