

Study Guide and Intervention

7MR3.3, 7AF1.1

Polygons and Angles

An **interior angle** is any angle that lies inside a polygon. A **regular polygon** is a polygon whose sides and angles are congruent.

Example 1 Find the sum of the measures of the interior angles of a tricontagon, which is a 30-sided polygon.

$$S = (n - 2)180^\circ \quad \text{Write an equation.}$$

$$S = (30 - 2)180^\circ \quad \text{Replace } n \text{ with 30. Subtract.}$$

$$S = (28)180^\circ \quad \text{Multiply.}$$

$$S = 5,040^\circ$$

The sum of the measures of the interior angles of a tricontagon is $5,040^\circ$.

Example 2 The defense department of the United States has its headquarters in a building called the Pentagon because it is shaped like a regular pentagon. What is the measure of an interior angle of a regular pentagon?

$$S = (n - 2)180^\circ \quad \text{Write an equation.}$$

$$S = (5 - 2)180^\circ \quad \text{Replace } n \text{ with 5. Subtract.}$$

$$S = (3)180^\circ \quad \text{Multiply.}$$

$$S = 540^\circ$$

$$540^\circ \div 5 = 108^\circ \quad \text{Divide by the number of interior angles to find the measure of one angle.}$$

The measure of one interior angle of a regular pentagon is 108° .

Exercises

For Exercises 1–6, find the sum of the measures of the interior angles of the given polygon.

- nonagon (9-sided) $1,260^\circ$
- 14-gon $2,160^\circ$
- 16-gon $2,520^\circ$
- hendecagon (11-sided) $1,620^\circ$
- 25-gon $4,140^\circ$
- 42-gon $7,200^\circ$

For Exercises 7–12, find the measure of one interior angle of the given polygon. Round to the nearest hundredth if necessary.

- hexagon 120°
- 15-gon 156°
- 22-gon 163.63°
- icosagon (20-sided) 162°
- 38-gon 170.53°
- pentacontagon (50-sided) 172.8°